

1. Given the original function $f(x)$ describe all the transformations that would occur to $g(x)$:

a. $f(x) = \sqrt{x}$ $g(x) = \sqrt{4x}$
 Horizontal shrink by 4

b. $f(x) = e^x$ $g(x) = -5e^x$
 Reflect over x-axis
 Vertical stretch by 5

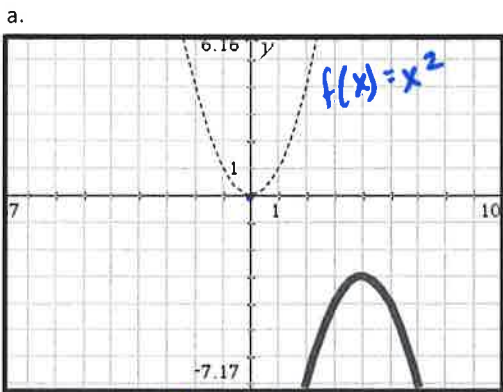
c. $f(x) = x^3$ $g(x) = (-x + 3)^3 + 7$
 Reflect over y-axis
 Left 3
 Up 7

d. $f(x) = |x|$ $g(x) = 0.1|-x - 1| - 5$
 Vertical shrink by 10
 Reflect over y-axis
 Right 1
 Down 5

e. $f(x) = \ln(x)$ $g(x) = -\ln\left(\frac{x}{2}\right)$
 Reflect over x-axis
 Horizontal stretch by 2

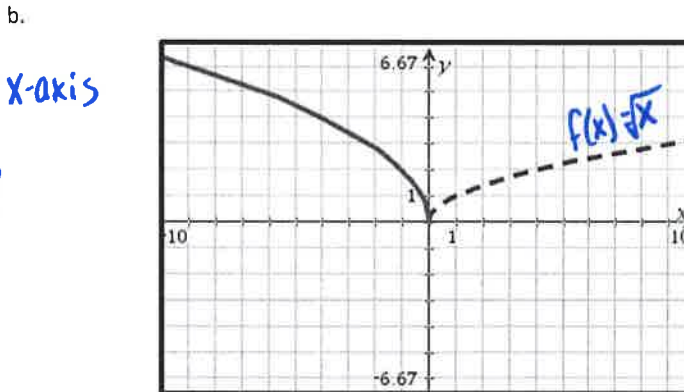
f. $f(x) = \sqrt[3]{x}$ $g(x) = -\sqrt[3]{-x}$
 Reflect over x-axis
 Reflect over y-axis

2. Based in the graph of the original function (dashed lines) write an equation that represents the graph of the transformed function (**bold lines**).



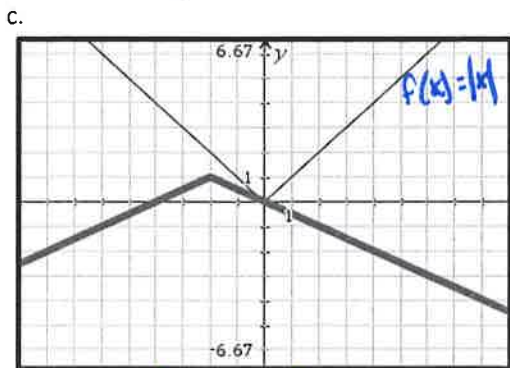
Ref. over x-axis
 Down 3
 Right 4

$g(x) = -(x-4)^2 - 3$



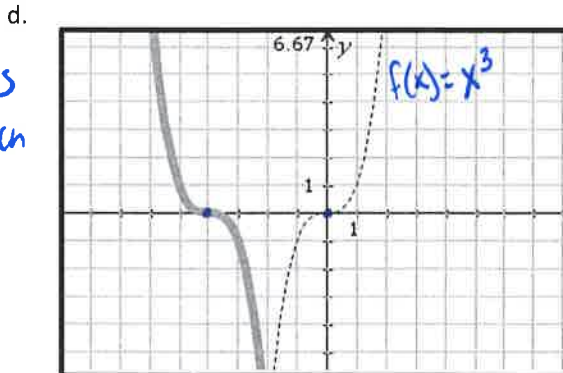
Ref. over y-axis
 Vertical stretch by 2

$g(x) = 2\sqrt{-x}$



Ref. over x-axis
 Horizontal stretch by 2
 Left 2
 Up 1

$g(x) = -\left|\frac{1}{2}x + 2\right| + 1$

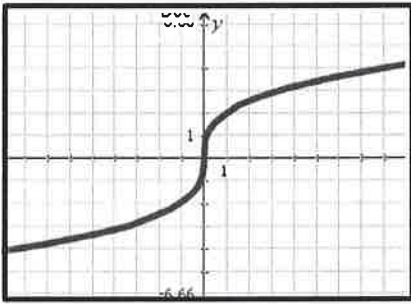


Ref. over x-axis
 Left 4

$g(x) = -(x+4)^3$

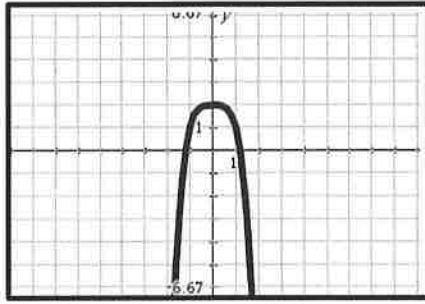
3. Based on the given graph determine if the function is *even*, *odd* or *neither*.

a.



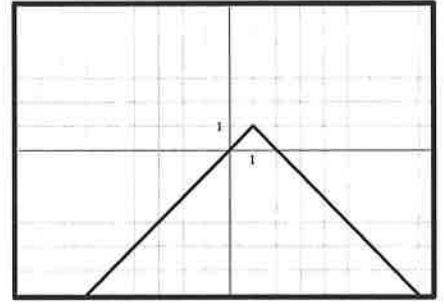
Odd (double reflect)

b.



Even (y-axis symmetry)

c.



Neither

4. Determine if the function is *even*, *odd* or *neither*. Justify your answer either algebraically or in sentence form.

a. $f(x) = -5x^3 + 9|x|$

$$f(-x) = -5(-x)^3 + 9|-x|$$

$$= 5x^3 + 9|x|$$

Neither

c. $f(x) = -x^5 - 9x^3 + \frac{1}{x}$

$$f(-x) = -(-x)^5 - 9(-x)^3 + \frac{1}{-x}$$

$$= x^5 + 9x^3 - \frac{1}{x}$$

odd

b. $f(x) = 9(x+2)(x-2) + 5 \rightarrow 9(x^2-4) + 5$

$$f(-x) = 9(-x)^2 - 31$$

$$= 9x^2 - 31$$

even

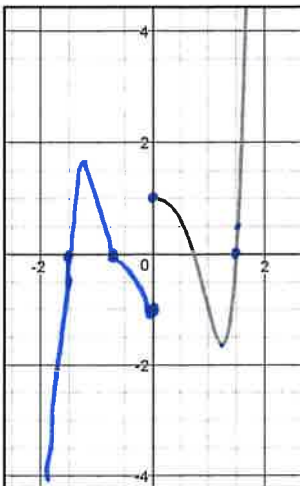
d. $f(x) = \sqrt{3x^4 + 2x^2 + 3}$

$$f(-x) = \sqrt{3(-x)^4 + 2(-x)^2 + 3}$$

$$= \sqrt{3x^4 + 2x^2 + 3} \text{ even}$$

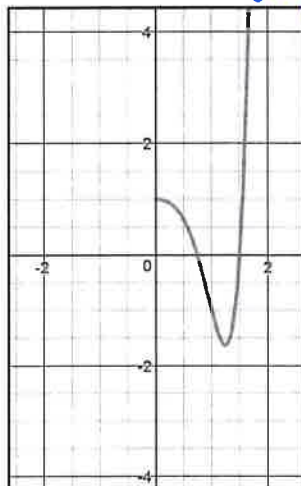
5. Complete the graph so that the function is the indicated type.

a. Odd

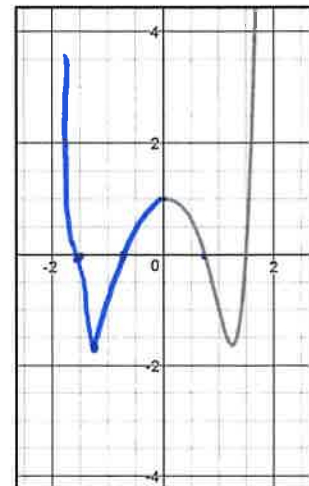


b. Neither

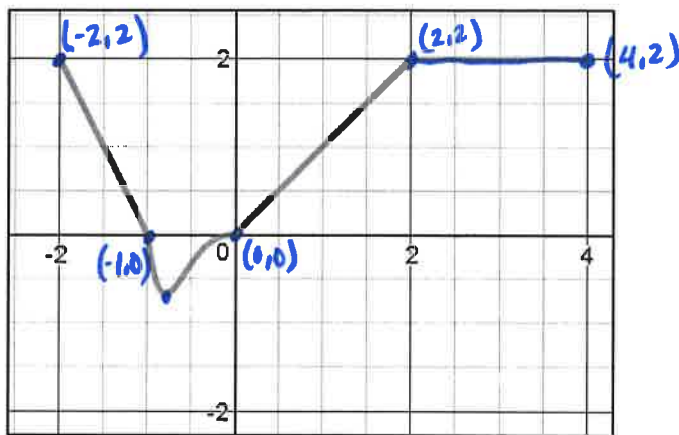
* answers vary



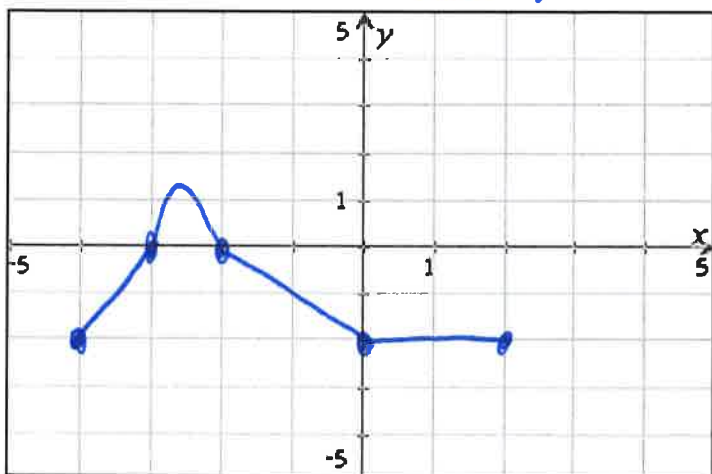
c. Even



6. A function, $f(x)$, is graphed below. Graph $g(x)$ correctly based on the transformations provided.

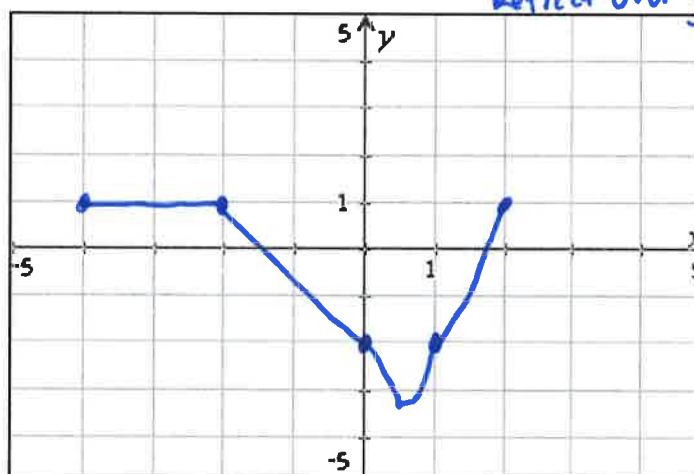


a. $g(x) = -f(x+2)$ Reflect over x, left + 2



$$\begin{aligned} (x, y) &\rightarrow (x-2, -y) \\ (-2, 2) &\rightarrow (-4, -2) \\ (-1, 0) &\rightarrow (-3, 0) \\ (0, 0) &\rightarrow (-2, 0) \\ (2, 2) &\rightarrow (0, -2) \\ (4, 2) &\rightarrow (2, -2) \end{aligned}$$

b. $g(x) = 1.5f(-x) - 2$ Vertical stretch, down 2, reflect over y



$$\begin{aligned} (x, y) &\rightarrow (-x, 1.5y-2) \\ (-2, 2) &\rightarrow (2, 1) \\ (-1, 0) &\rightarrow (1, -2) \\ (0, 0) &\rightarrow (0, -2) \\ (2, 2) &\rightarrow (-2, 1) \\ (4, 2) &\rightarrow (-4, 1) \end{aligned}$$