

### Honors PreCalculus

Sequences

A CO

### What's a sequence?

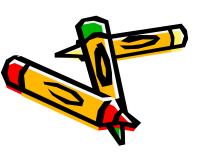
- An ordered progression of numbers
  - <u>Finite sequence</u>: 2,4,6,8,10
  - Infinite sequence: 1, 3, 9, ...,  $3^{k}$ , ...
  - <u>Fibonacci sequence:</u> 1, 1, 2, 3, 5, 8, 13, . . .



## What's a sequence?

- <u>Arithmetic sequence</u>
  - Numbers in the sequence have a <u>common</u> <u>difference</u>
    - <u>Add</u> or <u>subtract</u> the same number each time

• 
$$a_n = a_1 + (n - 1)d$$



# Arithmetic Sequences

#### Example 1:

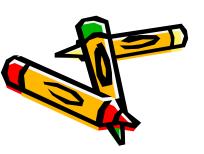
- Find the common difference, the rule (equation) and the 10<sup>th</sup> term of the sequence: -3, -1, 1, 3, 5, . . .
- Equation (rule):  $a_n = a_1 + (n 1)d$ 
  - a<sub>1</sub> = -3
  - d = 2
  - So:  $a_n = -3 + (n 1)(2) = -3 + 2n 2 = 2n 5$
  - 10<sup>th</sup> term: n = 10, so  $a_{10} = 2(10) 5 = 20 5 = 15$



## Arithmetic Sequences

#### Example 2:

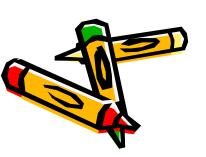
- Find the common difference, the rule (equation) and the 10<sup>th</sup> term of the sequence: 6, 2, -2, -6, -10, . . .
- Equation (rule):  $a_n = a_1 + (n 1)d$ 
  - a<sub>1</sub> = 6
  - d = -4
  - So:  $a_n = 6 + (n 1)(-4) = 6 4n + 4 = -4n + 10$
  - 10<sup>th</sup> term: n = 10, so  $a_{10} = -4(10) + 10 = -40 + 10 = -30$



# Constructing Sequences

#### Example 3:

If the 2<sup>nd</sup> and 5<sup>th</sup> terms of a sequence are 3 and 24, respectively, find the equation of the arithmetic sequence

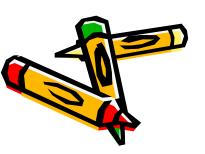


## What's a sequence?

- Geometric sequence
  - Numbers in the sequence have a <u>common</u> <u>ratio</u>
    - <u>Multiply</u> or <u>divide</u> by the same number each time
  - <u>General "rule"</u>

$$a_n = a_1(r^{n-1})$$

Q, -> first ferm



## Geometric Sequences

#### Example 4:

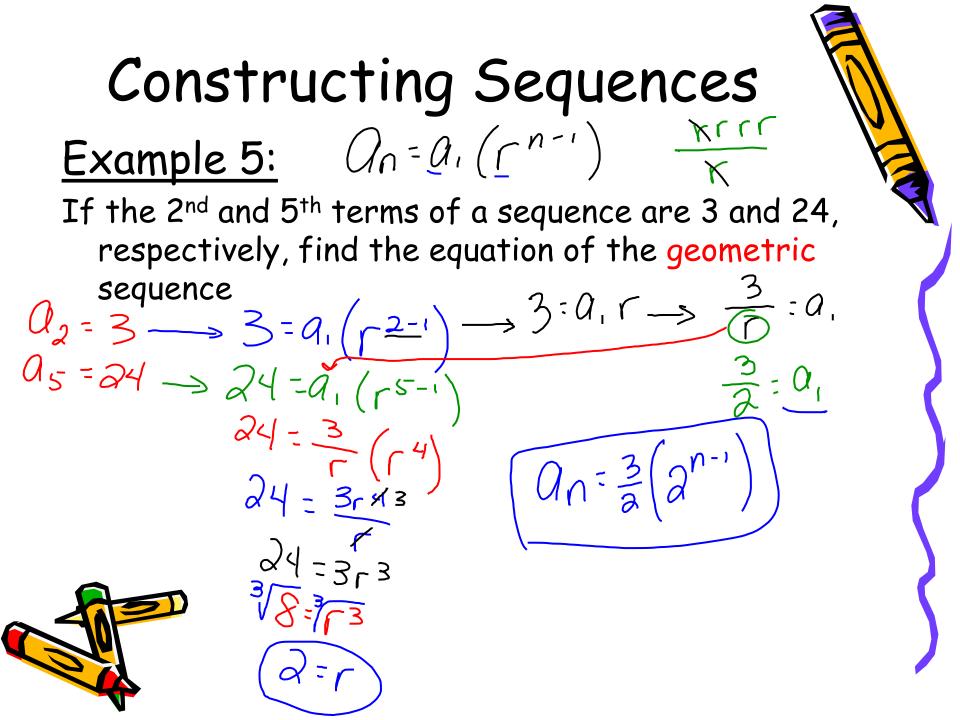
Find the common ratio, the rule (equation) and the 10<sup>th</sup> term of the sequence: 3, 6, 12, 24, 48, . . .

- Equation (rule):  $a_n = a_1(r^{n-1})$ 
  - a<sub>1</sub> = 3

- So 
$$a_n = 3(2^{n-1})$$

- 10<sup>th</sup> term: n = 10, so  $a_{10} = 3(2^{10-1}) = 3(2^9) = 1536$ 





### Limit of a sequence

A sequence <u>converges</u> if the numbers in the sequence approach a particular number

A sequence <u>diverges</u> if the numbers in the sequence approach infinity, or don't actually approach any particular number



